

1

... , 15, 49005, ; e-mail:office.itm@nas.gov.ua

... , 12/201008, ; e-mail:infomf@minfin.gov.ua

" - "

()

(

),

:

" - " " - "

()

(

Rocket hardware represents technically complex expensive and unique engineering systems. At present, decisions on the advisability of implementation of new rocket hardware development projects are made based on

© . . . , . . . , . . . , . . . 2018

. - 2018. - 2.

financial feasibility study materials with the use of the benefit–cost or cost–efficiency criterion without even rough quantitative estimates of cost overrun or efficiency reduction risks.

The methodological approach presented in this paper is a first stage in the development of mathematical methods and algorithms for calculating the expected engineering and economical performance characteristics of new rocket hardware development projects with account for risks.

This paper proposes an econometric model for calculating the expected cost of new rocket hardware development and assessing the risk of cost overrun and delay in the development work.

The mathematical model is based on an analytical relationship between the required performance characteristics of a new rocket product and its cost parameters.

To make the expected cost calculation and cost overrun risk assessment method more formal, the technical structure of a rocket system is represented as a weighted directed tree graph. The graph vertices are the rocket system itself (the root vertex) and its components. The graph arc weights are a tuple of the engineering and economical performance characteristics of the lower-level component included in the nearest vertex of the tree graph.

The risk of expected cost overrun and delay in the development work is due to uncertainty in the input data used in the calculation (the variables and the parameters of the econometric model). The data uncertainty is modeled using the fuzzy set theory: the model variables and parameters are represented as fuzzy triangular numbers.

Let $Z = \{z_1, z_2, \dots, z_n\}$ be a set of fuzzy triangular numbers, where $z_i = (a_i, b_i, c_i)$ is a fuzzy triangular number with vertices a_i, b_i, c_i and $i = 1, 2, \dots, n$.

[1].

Let $U = \{u_1, u_2, \dots, u_m\}$ be a set of fuzzy triangular numbers, where $u_j = (a_j, b_j, c_j)$ is a fuzzy triangular number with vertices a_j, b_j, c_j and $j = 1, 2, \dots, m$.

Let $V = \{v_1, v_2, \dots, v_k\}$ be a set of fuzzy triangular numbers, where $v_l = (a_l, b_l, c_l)$ is a fuzzy triangular number with vertices a_l, b_l, c_l and $l = 1, 2, \dots, k$.

Let $W = \{w_1, w_2, \dots, w_p\}$ be a set of fuzzy triangular numbers, where $w_r = (a_r, b_r, c_r)$ is a fuzzy triangular number with vertices a_r, b_r, c_r and $r = 1, 2, \dots, p$.

Let $X = \{x_1, x_2, \dots, x_q\}$ be a set of fuzzy triangular numbers, where $x_s = (a_s, b_s, c_s)$ is a fuzzy triangular number with vertices a_s, b_s, c_s and $s = 1, 2, \dots, q$.

Let $Y = \{y_1, y_2, \dots, y_r\}$ be a set of fuzzy triangular numbers, where $y_t = (a_t, b_t, c_t)$ is a fuzzy triangular number with vertices a_t, b_t, c_t and $t = 1, 2, \dots, r$.

$(Z);$

(U_z)

$$U_z = \langle \Delta Z, P(\Delta Z) \rangle,$$

ΔZ – $Z, P(\Delta Z)$ –
 $(Z + \Delta Z)$.

1,5 – 3

$\{\tau_M\}$

[2],

(UP) .

$$Z_{OKP} = f(\tau_1, \tau_2, \dots, \tau_m, \dots, \tau_M, P(UP)),$$

Z_{OKP} – $\tau_1, \tau_2, \dots, \tau_m, \dots, \tau_M,$ –
 $P(UP)$ –

...

$$G(V, W, E_V, E_W),$$

$$V = \langle V_0, V_1, V_2, \dots, V_N \rangle = \{V_n\}, n = \overline{0, N},$$

$$W = \langle W_0, W_1, W_2, \dots, W_S \rangle = \{W_s\}, s = \overline{1, S},$$

$\{V_n\}$ () $\{W_s\}$ () - $G, E_V - \{V_n\}, E_W - \{W_s\}$.

$$E_V = \langle E_{V1}, E_{V2}, \dots, E_{VN} \rangle = \{E_{Vn}\}, E_{Vn} = \langle e_{Vnq1}, e_{Vnq2}, \dots, e_{Vqi} \rangle,$$

$$E_W = \langle E_{W1}, E_{W2}, \dots, E_{WS} \rangle = \{E_{Ws}\}, E_{Ws} = \langle e_{Wsp1}, e_{Wsp2}, \dots, e_{Wspj} \rangle,$$

$$\begin{aligned} \mathfrak{A}_{Vnq1} &= \dots, & V_n & & V_{q1}; \\ \mathfrak{A}_{Wsp1} &= \dots, & W_s & & W_{p1} \\ & & & & V_{p1}. \end{aligned}$$

$$\begin{aligned} (\quad) & & & & * \{K_n\} \\ V = \{V_n\} & G, & & & I = \{I_s\} - \\ \{W_s\}. & & & & \end{aligned}$$

$$G(V, W, E_V, E_W). \quad V_0,$$

$$V_0 \quad G: \quad \rightarrow V_0.$$

$$\begin{aligned} (\quad), & & (\quad), & & \\ (\quad), & & (\quad), & & \\ & & I^0 = \{I_k^0\} (k = \overline{1, K}) & : & \\ (\quad), & & (\quad), & & \\ & & (\quad), & & \end{aligned}$$

$$\begin{aligned} G(V, W, E_V, E_W) \\ G(V, W^0, E_V, E_W^0) & G^0(W^0, W, E_W) = \{G_m^0(W_m^0, W, E_W)\}, \\ (m = \overline{1, M}). \end{aligned}$$

$$\begin{aligned} G(V, W^0, E_V, E_W^0) & \{V_n\} \\ & \{I_k^0\}, \\ -V_0. & \end{aligned}$$

$$\begin{aligned} G_m^0(W_m^0, W_m, E_W) & W_m^0 \\ (m = \overline{1, M}) \end{aligned}$$

$$G_m^0(W_m^0, W_m, E_W)$$

* $\{I_k^0\}$

$$Z_q = Z(K_q) + Z(EB_q), \quad Z(K_q) = \sum_{\alpha=1}^{\bar{q}_\alpha} Z(K_{q\alpha}) + \sum_{\beta=1}^{\bar{q}_\beta} Z(I_{q\beta}^0) + Z(TD_q),$$

$$Z(TD_q) = \frac{1}{q_\alpha + q_\beta} \left(\sum_{\alpha=1}^{\bar{q}_\alpha} Z(TD_{q\alpha}) + \sum_{\beta=1}^{\bar{q}_\beta} Z(TD_{q\beta}) \right) \cdot (1 + \delta_{TD}), \quad (1)$$

$$Z(EB_q) = \frac{1}{q_\alpha + q_\beta} \left(\sum_{\alpha=1}^{\bar{q}_\alpha} Z(EB_{q\alpha}) + \sum_{\beta=1}^{\bar{q}_\beta} Z(EB_{q\beta}) \right) \cdot (1 + \delta_{EB}),$$

$$Z_q(q=0) = Z(K_0) = \sum_{\alpha=1}^{Q_0} Z(K_{q\alpha}) \cdot (1 + \gamma_0 + \delta\gamma_0), \quad q = N - n,$$

Z_q ; $Z(K_q)$; $Z(EB_q)$; q ; $K_{q\alpha}$; $I_{q\beta}^0$; $Z(TD_q)$; q ; \bar{q}_α ; \bar{q}_β ; $I_{q\beta}^0$; q ; δ_{TD} ; δ_{EB} ; $Z_q(q_0) = Z(K_0)$; Q_0 ; γ_0 ; $\delta\gamma_0$; γ_0 .

$$q \text{ (} q = \{N, N-1, \dots, 1, 0\} \text{)}.$$

"0").

$$I^0 = \langle I_1^0, I_2^0, \dots, I_M^0 \rangle = \{I_m^0\},$$

$$(I_{mq}^0 \subset K_q).$$

$$G_m^0(W_m^0, W_m, E_{W_m}),$$

$$\bar{a}_m = (a_{1m}, a_{2m}, a_{3m}, a_{4m}),$$

$$W_m - G_m^0; E_{W_m} -$$

$$W_m; a_{1m} -$$

$$I_m; a_{2m} -$$

$$I_m; a_{3m} -$$

$$I_m; a_{4m} -$$

$$I_m.$$

$$a_{2m} > 0 \quad (0 < a_{2m} < 1),$$

$$a_{2m} = 0.$$

$$Z(I_m) = Z(I_m^a) \cdot K(t_0, t^a) \cdot \prod_{k=1}^{k_m} \left(\frac{\tau_k}{\tau_k^a} \right)^{\lambda_k^m},$$

$$Z(PD_m) = Z(I_m^a) \cdot \alpha_m^a \cdot k_\alpha(k_{Hm}, k_{TYm}) \cdot K(t^a, t_0),$$

$$Z(KTD_m) = Z(I_m^a) \cdot \beta_m^a \cdot k_\beta(k_{Hm}, k_{TYm}) \cdot K(t^a, t_0),$$

$$Z(EOH_m) = \eta_m(k_{Hm}, k_{TYm}) \cdot Z(EO_m^a) \cdot K(t^a, t_0) + Z(I_m^a) \cdot \gamma_m^a \cdot k(P_m),$$

$$k(P_m) = a_p \cdot \frac{\ln(1 - P_m)}{\ln(1 - P_m^a)},$$

$$Z(PP_m) = \theta_m(k_{Hm}, k_{TCm}) \cdot Z(PP_m^a) \cdot K(t_0, t^a),$$

$$Z(EB) = \vartheta_m(k_{Hm}, k_{TYm}) \cdot Z(EB_m^a) \cdot K(t_0, t^a), \quad (2)$$

$$Z(I_m^a) = Z(I_m^{a\phi}) \cdot (1 + \varepsilon_m),$$

$$\varepsilon_m \in [-\varepsilon_m^{\max}, \varepsilon_m^{\max}], \quad \varepsilon_m^{\max} = 1 - d_m,$$

$$Z(I_m^0) = \sum_{q=1}^{Q_n} Z(I_{mq}) \cdot (1 + \gamma_{mo}^a),$$

$$Z(I_m) = Z(I_m^a) \cdot K(t_0, t^a) \cdot \prod_{k=1}^{k_m} \left(\frac{\tau_k}{\tau_k^a} \right)^{\lambda_k^m},$$

$$Z(PD_m) = Z(I_m^a) \cdot \alpha_m^a \cdot k_\alpha(k_{Hm}, k_{TYm}) \cdot K(t^a, t_0),$$

$$Z(KTD_m) = Z(I_m^a) \cdot \beta_m^a \cdot k_\beta(k_{Hm}, k_{TYm}) \cdot K(t^a, t_0),$$

$$Z(EOH_m) = \eta_m(k_{Hm}, k_{TYm}) \cdot Z(EO_m^a) \cdot K(t^a, t_0) + Z(I_m^a) \cdot \gamma_m^a \cdot k(P_m),$$

$$Z(PP_m) = \theta_m(k_{Hm}, k_{TCm}) \cdot Z(PP_m^a) \cdot K(t_0, t^a),$$

$$Z(EB) = \vartheta_m(k_{Hm}, k_{TYm}) \cdot Z(EB_m^a) \cdot K(t_0, t^a),$$

$$Z(I_m^a) = Z(I_m^{a\phi}) \cdot (1 + \varepsilon_m),$$

$$\varepsilon_m \in [-\varepsilon_m^{\max}, \varepsilon_m^{\max}], \quad \varepsilon_m^{\max} = 1 - d_m,$$

$$Z(I_m^0) = \sum_{q=1}^{Q_n} Z(I_{mq}) \cdot (1 + \gamma_{mo}^a),$$

$$I_m; Z(EOH_m) - ; Z(EO_m^a) - I_m^a; k(P_m) -$$

$$I_m P_m^a ; P_m; P_m, P_m^a - ; Z(PP_m), Z(PP_m^a) -$$

$$; k_{TCm} -$$

$$Z(EB_m), Z(EB_m^a) - ; Z(I_m^{a\phi}) -$$

$$I_m^a; \epsilon_m -$$

$$; d_m - ; Z(I_m^0) - I_m ; \lambda_k^m -$$

$$I_{mq},$$

$$\alpha_m^a, \beta_m^a, \gamma_m^a, \eta_m, \theta_m, \vartheta_m, \gamma_m^a, \gamma_{mo}^a, k_\alpha, k_\beta, a_p -$$

(2)

$$I_m^0,$$

(2)

$$I_m^0 (1).$$

$$St(I^*) = St(I) \cdot (1 + \delta(I)) \cdot (1 - \alpha - \delta_\alpha) \cdot K(t, t_0),$$

$$Z(I^*) = (St(I^*) \cdot (\beta_1 \cdot P_{ps} \cdot (1 + h_1) + \beta_2) \cdot (1 + h_2) \cdot (1 + h_3) +$$

$$+ \beta_3 \cdot \mu_1 \cdot (t + h_3) + \beta_3 \cdot (1 - \mu_1)) \cdot \prod_{s=1}^S \left(\frac{\tau_s}{\tau_s^a} \right)^{\lambda_s} \cdot q_V(t_0),$$

$$Z(I) = Z(I^*) + \sum G_\tau, \quad Z(PD) = \mu_2 \cdot Z(I),$$

$$Z(KTD) = \mu_3 \cdot Z(I), \quad Z(EO) = \mu_4 \cdot Z(I),$$

$$St(I^*) - ; St(I) - t_0 -$$

$\delta(I) -$
 $\alpha -$; $\delta_\alpha -$
 $\alpha; \alpha_1 -$
 $I; K(t, t_0) -$
 $t_0; Z(I^*) -$
 $\beta_1 -$
 $P_{ps} -$
 $h_1 -$;
 $\beta_2 -$
 $h_1 -$; $h_3 -$
 $\beta_3 -$
 $\tau_s, \tau_s^a -$
 $\lambda_s -$
 $q_v(t_0) -$; $Z(I) -$
 $\sum G_\tau -$; $Z(PD) -$
 $Z(KTD) -$; $Z(EO) -$; $\mu_1, \mu_2, \mu_3, \mu_4 -$
 $I .$
 $(\Delta Z_{OKP});$
 $(\Delta T_{OKP});$
 $(\Delta K_{TЭ});$
 $(\Delta P_E);$
 $(\Delta I_S).$

$$\mu(x) < 1 \quad \forall x \in [a_{\min}, a_{\max}] \quad \mu(x) = 0, \quad x \notin [a_{\min}, a_{\max}]. \quad [3].$$

$$q_x \in [a_{\min}, a_{\max}]. \quad (SR)$$

$$\mu(x) \quad [4].$$

$$SG(t_{ij}, RB_{ij}) = \frac{(\Delta T_{OKP})}{RB_{ij}} \quad (i, j)$$

$i -$

$),$

$),$

(t_{\min})

(t_{\max})

t_{ij}

$t_{ij} \cdot$

$t_{ij} :$

$$t_{ij} = \begin{cases} t_{ij}^0 = \frac{t_{\min} + t_{\max}}{2} \\ t_{ij} \end{cases}$$

T_{kp}^0

T_{kp}^{\max}

$T_{kp}^0 :$

$$T_{OKP} = T_{kp}^0$$

$$T_{кр}^{\max} - T_{кр}^0 = \Delta T_{ОКР}$$

$$T_{кр}^0$$

$$T_{кр}^{\max}$$

$$T_{ОКР}^{\max} = T_{ОКР}^0 \cdot d_t, \quad d_t = a_t \cdot (\exp(b_t x_t)), \quad x_t = (1 + k_{HK})^\alpha \cdot (1 + k_{TC})^\beta,$$

$$T_{ОКР}^0 \quad - \quad ; \quad a_t \quad b_t \quad -$$

$$; \quad x_t \quad - \quad ; \quad k_{HK} \quad -$$

$$; \quad k_{TC} \quad -$$

$$; \quad \alpha \quad -$$

$$k_{HK} ; \quad \beta \quad -$$

$$k_{TC} \cdot$$

$$\Delta T_{ОКР} = (1 - d_t) T_{ОКР}^0 \cdot$$

[2].

(2-4

).

()

()

1. 2015. 3. 3-17.
2. : , 2008. 509 .
3. : , 1990.
4. 2016. 2. . 137-146.

21.05.2018,
30.05.2018