

# FLUCTUATIONS AND ION-ACOUSTIC WAVES IN COLLISIONAL DUSTY PLASMA WITH VARIABLE GRAIN CHARGE

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The kinetic theory of electric fluctuations in a collisional weakly ionized dusty plasma is formulated with regard to the grain charge variations. The spectra of ion-acoustic wave and of electron density correlation in nonisothermal plasmas are calculated for various values of grain density and grain size.

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## INTRODUCTION

The theory of fluctuations in the ordinary collisional plasma is well developed [1-5]. The problem of generalization of this theory to the case of dusty plasma has a number of issues remained open. The dust grains acquire electric charges due to absorption of electrons and ions from the surrounding plasma i.e. grains are charged by the plasma currents that flow toward its surface. In the stationary state, the flux of electrons on the grain surface is equal to the flux of ions, thus the total current is equal to zero. The fluctuations of the charging current lead to the fluctuations of the stationary grain charge. Moreover, since the grain charges depend on electromagnetic field via charging currents, they generate additional dielectric response of the medium, which can influence the propagation of electromagnetic waves in dusty plasma.

The major part of the results for fluctuations [6-9] and ion-acoustic waves [10-12] are obtained for collisionless dusty plasmas. However, this approximation is not applicable for dusty plasma experimental conditions [13, 14].

The purpose of the present paper is to give a consistent linear kinetic description of electric fluctuations and dielectric response in collisional weakly ionized dusty plasma with regard to the absorption of electrons and ions by grains and grain charge variations.

## 1. GRAIN CHARGE FLUCTUATIONS

The charge density fluctuations in a dusty plasma include fluctuations related to electrons and ions  $\delta\rho_\alpha(\mathbf{r}, t) = e_\alpha \delta n_\alpha(\mathbf{r}, t)$ ,  $\alpha = e, i$ , as well as the grain charge density fluctuations

$$\delta\rho_g(\mathbf{r}, t) = e_g \delta n_g(\mathbf{r}, t) + n_g \delta e_g(\mathbf{r}, t), \quad (1)$$

where  $e_g$  is the stationary grain charge and  $n_g$  is the mean number density of grains. Such representation is valid for fluctuations that satisfy the condition  $n_g R^3 \gg 1$ , where  $R$  is the spatial scale of perturbation. The number density fluctuations of charged particles have the form

$$\delta n_\alpha(\mathbf{r}, t) = n_\alpha \int d\mathbf{v} \delta f_\alpha(\mathbf{r}, \mathbf{v}, t), \quad \alpha = e, i, g, \quad (2)$$

where  $\delta f_\alpha(\mathbf{r}, \mathbf{v}, t)$  are the fluctuations of distribution function. In the case of electrons or ions, they can be

found in the same way as in ordinary plasma [5], but regarding the collisions of electrons and ions with grains in addition to collisions with neutrals.

Fluctuations of electron and ion distribution functions satisfy the equation [5]

$$\left\{ \frac{\partial}{\partial t} + \mathbf{v} \frac{\partial}{\partial \mathbf{r}} \right\} \delta f_\alpha(X, t) + \nu_\alpha \{ \delta f_\alpha(X, t) - f_{0\alpha}(\mathbf{v}) \int d\mathbf{v}' \delta f_\alpha(X, t) \} = - \frac{e_\alpha}{m_\alpha} \frac{\partial \delta\phi(\mathbf{r}, t)}{\partial \mathbf{r}} \frac{\partial f_{0\alpha}(\mathbf{v})}{\partial \mathbf{v}}, \quad (3)$$

where  $X = (\mathbf{r}, \mathbf{v})$ ,  $\delta\phi(\mathbf{r}, t)$  is the fluctuation of electrostatic potential,  $f_{0\alpha}(\mathbf{v})$  is the unperturbed distribution function,  $\nu_\alpha = \nu_{\alpha n} + \nu_{\alpha g}$ , and  $\nu_{\alpha n}$ ,  $\nu_{\alpha g}$  are the effective collision frequencies between particles of  $\alpha$  species with neutrals and grains. We assume that the electrons and ions absorbed by the grain recombine on its surface and form the neutral gas atoms that evaporate into the surrounding plasma and can be ionized again. Such assumption makes it possible to use the Bhatnagar-Gross-Krook (BGK) collision integral [16] in Eq. (3).

The averaging of the equation for microscopic phase density of grains results into kinetic equation with collision integral that can be expressed in terms of the correlation functions of microscopic quantities [5]. The linearized equation for the fluctuations of grain distribution function has the form of Eq. (3) with  $\alpha = g$ , where  $\nu_g$  is the effective collision frequency between grains and other particles.

The formal solution of Eq. (3) is given by

$$\delta f_\alpha(X, t) = \delta f_\alpha^{(0)}(X, t) - \frac{e_\alpha}{m_\alpha} \int_{-\infty}^t dt' \int dX' W_\alpha(X, X'; t-t') \frac{\partial \delta\phi(\mathbf{r}', t')}{\partial \mathbf{r}'} \frac{\partial f_{0\alpha}(\mathbf{v}')}{\partial \mathbf{v}'}, \quad (4)$$

where  $\delta f_\alpha^{(0)}(X, t)$  is the general solution of the homogenous Eq. (3),  $W_\alpha(X, X'; t-t')$  also satisfies the homogenous Eq. (3), but with the initial condition  $W_\alpha(X, X'; 0) = \delta(X - X')$ .

We also need to describe the dynamics of grain charge fluctuations  $\delta e_g(\mathbf{r}, t)$ . Following the Ref. [15], we assume that

$$\frac{\partial e_g(\mathbf{r}, t)}{\partial t} = \sum_{\alpha=e,i} I_{\text{ch}}^\alpha(n_\alpha(\mathbf{r}, t), e_g(\mathbf{r}, t)). \quad (5)$$

For the small fluctuations of the grain charge  $\delta e_g(\mathbf{r}, t)$  from its stationary value  $e_g$ , which is determined by the condition of zero total charging current  $I_{\text{ch}}^i + I_{\text{ch}}^e = 0$ , (5) gives the equation for  $\delta e_g(\mathbf{r}, t)$

$$\frac{\partial \delta e_g(\mathbf{r}, t)}{\partial t} + \nu_{\text{ch}} \delta e_g(\mathbf{r}, t) = \sum_{\alpha=e,i} \frac{\partial I_{\text{ch}}^\alpha(n_\alpha, e_g)}{\partial n_\alpha} \delta n_\alpha(\mathbf{r}, t), \quad (6)$$

where  $\nu_{\text{ch}}$  is the charging frequency

$$\nu_{\text{ch}} = \sum_{\alpha=e,i} \nu_{\text{ch}}^\alpha, \quad \nu_{\text{ch}}^\alpha = -\frac{\partial I_{\text{ch}}^\alpha(n_\alpha, e_g)}{\partial e_g}. \quad (7)$$

Now, the explicit form of charging currents  $I_{\text{ch}}^\alpha(n_\alpha, e_g)$  in collisional plasma is needed. Since the mean free path of electrons  $l_e$  is, usually, about two orders higher than  $l_i$ , we use the expression

$$I_{\text{ch}}^e = e_e n_e \sqrt{8\pi a^2 \nu_{Te}} \exp(-\alpha), \quad (8)$$

which is obtained in orbit motion limited (OML) approximation, i.e. the collisions of electrons with neutrals are neglected.

For ionic charging current we use the interpolation formula [17], which reproduce with high accuracy the results of kinetic calculations [18]

$$I_{\text{ch}}^i = e_i n_i \sqrt{8\pi a^2 \nu_{Ti}} \frac{I_{\text{ch}}^{\text{WC}} I_{\text{ch}}^{\text{SC}}}{I_{\text{ch}}^{\text{WC}} + I_{\text{ch}}^{\text{SC}}}, \quad (9)$$

where

$$I_{\text{ch}}^{\text{WC}} = 1 + \alpha\tau + 0.1(\alpha\tau)^2 \lambda_D / l_i, \quad (10)$$

$$I_{\text{ch}}^{\text{SC}} = \sqrt{2\pi\alpha\tau} l_i / a, \quad \tau = T_e / T_i. \quad (11)$$

Here  $\alpha = e_e \phi_s / T_e$  (not to be confused with subscript  $\alpha$  that denotes the plasma particle species),  $\phi_s$  is the surface potential,  $a$  is the grain radius,  $k_D^2 = k_{De}^2 + k_{Di}^2$ ,  $k_{D\alpha}^2 = 4\pi e_\alpha^2 n_\alpha / T_\alpha$ ,  $\lambda_D = 1/k_D$  is the Debye length,  $\nu_{T\alpha} = \sqrt{T_\alpha / m_\alpha}$  is the plasma particle thermal velocity,  $l_i = \nu_{Ti} / \nu_i$  is the ion mean free path,  $\nu_i$  is the collision frequency of ions with other particles. WC stands for weakly collisional and SC is for strongly collisional.

It is reasonable to assume [18-22] that the electrostatic potential near the grain is described by the Derjaguin-Landau-Verwey-Overbeek (DLVO) potential, then

$$\alpha = \frac{e_e e_g}{a T_e (1 + a k_D)}. \quad (12)$$

The space-time Fourier transform (FT) of Eq. (1) for the grain charge fluctuations along with (6) gives

$$\delta \rho_{g\mathbf{k}\omega} = e_g \delta n_{g\mathbf{k}\omega} + \frac{i n_g}{\omega + i \nu_{\text{ch}}} \sum_{\alpha=e,i} \frac{I_{\text{ch}}^\alpha}{n_\alpha} \delta n_{\alpha\mathbf{k}\omega}. \quad (13)$$

We substitute (4) in (2) and after FT obtain

$$\delta n_{\alpha\mathbf{k}\omega} = \delta n_{\alpha\mathbf{k}\omega}^{(0)} - \frac{k^2}{4\pi e_\alpha} \chi_\alpha(\mathbf{k}, \omega) \delta \phi_{\mathbf{k}\omega}, \quad \alpha = e, i, g, \quad (14)$$

where  $\chi_\alpha(\mathbf{k}, \omega)$  is the dielectric susceptibility.

And substituting (14) with  $\alpha = g$  in the first term of (13) and with  $\alpha = e, i$  in the second one, we obtain

$$\delta \rho_{g\mathbf{k}\omega} = \delta \rho_{g\mathbf{k}\omega}^{(0)} - \frac{k^2}{4\pi} \chi_g(\mathbf{k}, \omega) \delta \phi_{\mathbf{k}\omega} + \frac{i}{\omega + i \nu_{\text{ch}}} \times \\ \times \sum_{\alpha=e,i} \nu_{\alpha g} \delta \rho_{\alpha\mathbf{k}\omega}^{(0)} - \frac{k^2}{4\pi} \frac{i}{\omega + i \nu_{\text{ch}}} \sum_{\alpha=e,i} \nu_{\alpha g} \chi_\alpha(\mathbf{k}, \omega) \delta \phi_{\mathbf{k}\omega}, \quad (15)$$

where  $\nu_{\alpha g} = n_g I_{\text{ch}}^\alpha / (e_\alpha n_\alpha)$  is the frequency of plasma particle collisions with grains.

Thus,

$$\delta \phi_{\mathbf{k}\omega} = \frac{4\pi \delta \rho_{\mathbf{k}\omega}^{(0)}}{k^2 \varepsilon(\mathbf{k}, \omega)}, \quad (16)$$

where

$$\delta \rho_{\mathbf{k}\omega}^{(0)} = \sum_{\alpha=e,i,g} \delta \rho_{\alpha\mathbf{k}\omega}^{(0)} + \frac{i}{\omega + i \nu_{\text{ch}}} \sum_{\alpha=e,i} \nu_{\alpha g} \delta \rho_{\alpha\mathbf{k}\omega}^{(0)}, \quad (17)$$

$$\varepsilon(\mathbf{k}, \omega) = 1 + \sum_{\alpha=e,i,g} \chi_\alpha(\mathbf{k}, \omega) + \frac{i}{\omega + i \nu_{\text{ch}}} \sum_{\alpha=e,i} \nu_{\alpha g} \chi_\alpha(\mathbf{k}, \omega). \quad (18)$$

We see that the presence of grains lead to renormalization of the dielectric response and collisions with grains should be taken into account on equal footing with the collisions with neutrals, i.e.  $\nu_\alpha = \nu_{\alpha n} + \nu_{\alpha g}$ .

## 2. FLUCTUATION AND WAVE SPECTRA

It follows from (14), (16) and (17) that

$$\langle \delta \rho_e^2 \rangle_{\mathbf{k}\omega} = \left| 1 - \frac{\chi_e(\mathbf{k}, \omega)}{\varepsilon(\mathbf{k}, \omega)} \left( 1 + \frac{i \nu_{eg}}{\omega + i \nu_{\text{ch}}} \right) \right|^2 \langle \delta \rho_e^{(0)2} \rangle_{\mathbf{k}\omega} + \\ \left| \frac{\chi_e(\mathbf{k}, \omega)}{\varepsilon(\mathbf{k}, \omega)} \left( 1 + \frac{i \nu_{ig}}{\omega + i \nu_{\text{ch}}} \right) \right|^2 \langle \delta \rho_i^{(0)2} \rangle_{\mathbf{k}\omega} + \left| \frac{\chi_g(\mathbf{k}, \omega)}{\varepsilon(\mathbf{k}, \omega)} \right|^2 \langle \delta \rho_g^{(0)2} \rangle_{\mathbf{k}\omega} \quad (19)$$

where  $\langle \delta \rho_\alpha^{(0)2} \rangle_{\mathbf{k}\omega} = T_\alpha k^2 \text{Im} \chi_\alpha(\mathbf{k}, \omega) / (2\pi\omega)$  [23].

For the dielectric susceptibility of collisional plasma we use the results obtained [16] on the basis of kinetic equations with the BGK collision integral

$$\chi_\alpha(\mathbf{k}, \omega) = \frac{k_{D\alpha}^2}{k^2} \frac{(\omega + i \nu_\alpha) W(z_\alpha)}{\omega + i \nu_\alpha W(z_\alpha)}, \quad (20)$$

where  $z_\alpha = (\omega + i \nu_\alpha) / k \nu_{T\alpha}$  and  $W(z)$  is the plasma dispersion function.

The propagation of longitudinal waves in plasma can be studied by solving the dispersion equation

$$\varepsilon(\mathbf{k}, \omega) = 0, \quad (21)$$

which determines the eigenfrequency as a function of wave vector  $\omega(\mathbf{k})$ . For the real  $\mathbf{k}$ , the eigenfrequency is complex  $\omega(\mathbf{k}) = \omega_{\mathbf{k}} + i \gamma_{\mathbf{k}}$ , where  $\gamma_{\mathbf{k}}$  is the damping rate.

Below we present, the results of numerical solution of the dispersion equation (21) with dielectric permittivity (18) disregarding  $\chi_g(\mathbf{k}, \omega)$  and numerical calculations of electron density fluctuation spectra given by (19) for nonisothermal argon plasma ( $\tau = 100$ ).

The charging currents are the functions of parameter  $\alpha$  (12), which can be referred as normalized grain charge, it, in turn, is determined by the condition of zero total current on the grain surface  $I_{\text{ch}}^i + I_{\text{ch}}^e = 0$

$$\frac{n_e}{n_i} \sqrt{\tau \frac{m_i}{m_e}} \exp(-\alpha) = \frac{I^{wc} I^{sc}}{I^{wc} + I^{sc}}. \quad (22)$$

The ratio  $n_e/n_i$  in Eq. (22) is defined by the quasineutrality condition, which in the case of dusty plasma has the form  $e_e n_e + e_i n_i + e_g n_g = 0$ . For the singly charged ions  $n_e/n_i = 1 - P$ ,  $P = e_g n_g / e_e n_i$ , where  $P$  is the Havnes parameter, which describes the part of electron charge collected by dust.

Spectra and damping of ion-acoustic waves in dusty plasma with regard to grain charge fluctuations (solid lines in Fig. 1,a,b) are studied using the numerical solution of the dispersion equation where dielectric permittivity is given by the expression (18) disregarding  $\chi_g(\mathbf{k}, \omega)$ .

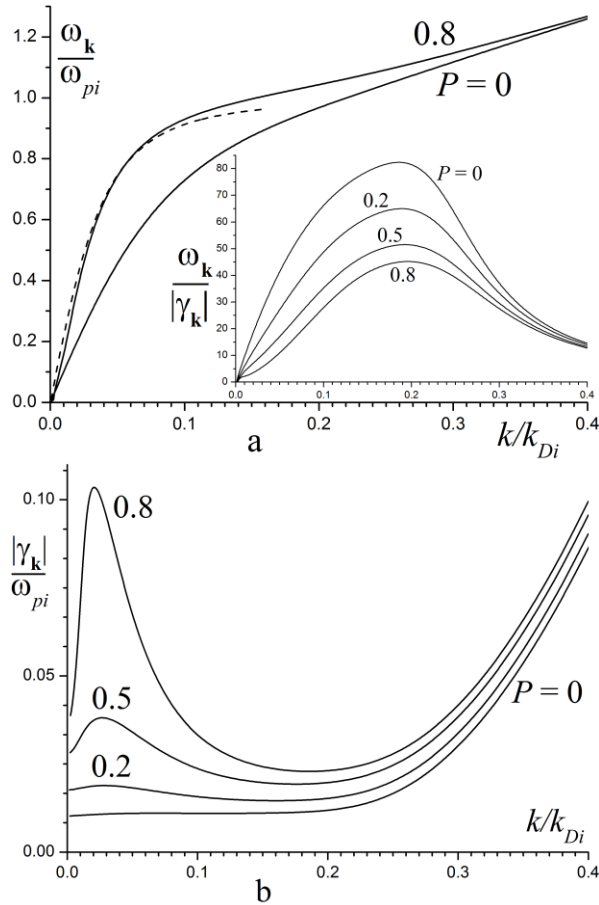


Fig. 1. Eigenfrequencies  $\omega_k$  (a) and absolute values of damping rates  $|\gamma_k|$  (b) of ion-acoustic waves in nonisothermal ( $\tau = 100$ ) argon dusty plasma vs wave number for  $v_{in} = 0.02\omega_{pi}$ ,  $ak_D = 0.15$ ,  $P = 0, 0.2, 0.5, 0.8$  (solid lines). Dashed lines corresponds to ordinary plasma, but with  $P = 0.8$ , insert is the ratio  $\omega_k/|\gamma_k|$

The possibility of the existence of ion-acoustic waves in isothermal collisionless dusty plasma was discussed for the first time in Ref. [24] and later they were discovered experimentally [25]. The Fig 1a shows that dispersion in dusty plasma is close to that one for ordinary plasmas, but with account to the change of  $n_e/n_i$  ( see dashed line in Fig. 1,a). Thus, grain charge

fluctuations and the increase of  $v_i$  due to collisions with grains do not affect the dispersion of ion-acoustic waves for the parameters under consideration.

Since the phase velocity of ion-acoustic wave is much higher than thermal velocity for  $\tau = 100$ , then the Landau damping is small for  $k \ll k_{De}$ , the additional increase of phase velocity due to the decrease of  $n_e/n_i$  does not affect the wave damping. In contrast, grain charge fluctuations and the increase of  $v_i$  lead to a considerable increase of the absolute value of damping rate (per order for  $k/k_{Di} \approx 0.02$ ) and to a decrease of the  $\omega_k/|\gamma_k|$  ratio accordingly (see insert in Fig. 1,a).

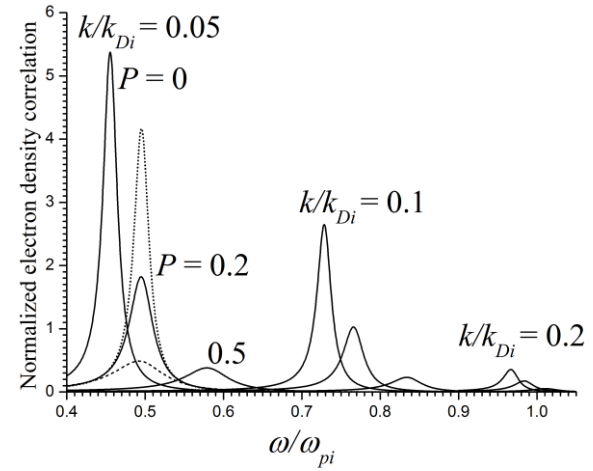


Fig. 2. Normalized electron density correlation spectra  $\langle \delta n_{\alpha}^2 \rangle_{k\omega} \omega_{pi} / n_i$  in nonisothermal ( $\tau = 100$ ) argon plasma for  $v_{in} = 0.02\omega_{pi}$ ,  $a/\lambda_D = 0.15$ ,  $k/k_{Di} = 0.05, 0.1, 0.2$ ,  $P = 0, 0.2, 0.5$ ,  $a/\lambda_D = 0.01$  (dotted line) and  $a/\lambda_D = 1$  (dashed line)

The fluctuation spectra in strongly nonisothermal ( $\tau = 100$ ) plasma, which are presented in Fig. 2, show that positions and intensities of maxima depend on the wave number  $k/k_{Di}$  and coincide with eigenfrequency of ion-acoustic waves (see Fig. 1,a). The presence of grains leads to the shift of fluctuation maxima toward higher frequencies and to decrease of fluctuation intensity

## CONCLUSIONS

The electron density correlation spectra are strongly affected by the presence of grains with variable charge. In the case of nonisothermal plasmas the positions of the ion-acoustic resonances and their intensities depend on Havnes parameter. Namely, the fluctuations of grain charges along with the increase of ion effective collision frequency suppress the electron density correlations. This effect is considerably depends on the grain size and is more pronounced for bigger grains. The decrease of electron to ion density ratio  $n_e/n_i$  in dusty plasma leads to the shift of fluctuation maxima to higher frequencies.

The dispersion of ion-acoustic waves is mostly affected by the decrease of electron to ion density ratio  $n_e/n_i$  in dusty plasma. The collisions between plasma particles and grains as well as the charge fluctuations are additional mechanisms of wave energy dissipation

and lead to a considerable growth of the absolute value of damping rate.

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## ФЛУКТУАЦИИ И ИОННО-ЗВУКОВЫЕ ВОЛНЫ В ПЫЛЕВОЙ СТОЛКНОВИТЕЛЬНОЙ ПЛАЗМЕ С ПЫЛИНКАМИ ПЕРЕМЕННОГО ЗАРЯДА

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Кинетическая теория электрических флуктуаций в столкновительной слабоионизированной пылевой плазме сформулирована с учетом переменного заряда пылинок. Рассчитаны спектры ионно-звуковых волн и корреляций электронной концентрации в неизотермической плазме для разных значений концентрации и размеров пылинок.

## ФЛУКТУАЦІЇ ТА ІОННО-ЗВУКОВІ ХВИЛІ В ЗАПОРОШЕНІЙ ЗІТКНЕННІЙ ПЛАЗМІ З ПОРОШИНКАМИ ЗМІННОГО ЗАРЯДУ

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Кінетична теорія електричних флуктуацій в зіткненій слабоіонізованій запорошеній плазмі сформульована з урахуванням змінного заряду порошинок. Розраховані спектри іонно-звукових хвиль і кореляцій електронної концентрації в неизотермічній плазмі для різних значень концентрації і розмірів порошинок.